1. Apply the Euclidean algorithm and calculate

$$\gcd(26,9)\qquad\qquad\qquad \gcd(81,18)$$

2. Express the following pairs of numbers in the form of Bezout identity

$$\alpha a + \beta b = \gcd(a, b)$$
.

$$(60, 12) (12, 18) (26, 9)$$

3. Find multiplicative modular inverse

2^{-1} in \mathbb{Z}_7	4^{-1} in \mathbb{Z}_{11}
9^{-1} in \mathbb{Z}_{26}	2^{-1} in \mathbb{Z}_6

4. Find additive inverse

$$-3 \text{ in } \mathbb{Z}_5$$
 $-4 \text{ in } \mathbb{Z}_{10}$

5. How many invertible elements?

$$\mathbb{Z}_6$$
 \mathbb{Z}_6^{\times} \mathbb{Z}_{11}^{\times}

6. Which elements have multiplicative inverses in \mathbb{Z}_8 and \mathbb{Z}_{20} ?

7. Write out addition and multiplication tables in \mathbb{Z}_5 and \mathbb{Z}_8 .

8. Which numbers are invertible in \mathbb{Z}_8 and \mathbb{Z}_{20} ?

9. Solve the following linear equations

$$\begin{array}{ll} x+3 \equiv 2 \pmod{5} & 5+6 \equiv x \pmod{11} & 5x+2 \equiv 3 \pmod{7} \\ 4x+3 \equiv 11 \pmod{12} & x-4 \equiv 7 \pmod{12} & 4x \equiv 2 \pmod{19} \\ 4x+3 \equiv 5 \pmod{13} & 2x+1 \equiv 9x-4 \pmod{23} & 5x-1 \equiv 3x+1 \pmod{26} \end{array}$$

10. Solve the systems of linear equations

$$\begin{cases} a+b \equiv 17 \pmod{26} \\ 2a+b \equiv 0 \pmod{26} \end{cases} \qquad \begin{cases} a+b \equiv 17 \pmod{26} \\ 4a+b \equiv 1 \pmod{26} \\ 4a+b \equiv 1 \pmod{26} \\ 3a+b \equiv 0 \pmod{26} \end{cases} \qquad \begin{cases} a+b \equiv 17 \pmod{26} \\ 16a+b \equiv 10 \pmod{26} \\ 16a+b \equiv 10 \pmod{26} \\ 5a+b \equiv 13 \pmod{26} \end{cases}$$